

# INDEX

## A

accuracy, and trigonometric questions xv  
addition rule for probabilities 210  
adjacent (right-angled triangle) xiii  
algebraic equations ix–x  
algebraic expressions, manipulating ix  
amplitude 158, 159, 163  
'and' in probability questions 205  
angle of depression xv  
of elevation xv  
of inclination of a line 29  
sum and difference identities 181–3  
arc length 33, 36, 43–49  
area of a triangle xiv  
given two sides and the angle between them 9–12  
asymptotes 136, 138

## B

bearings xv  
binomial expansion 243

## C

chord length 33, 34  
co-domain 53  
collinear points 19  
combinations 239–42  
and Pascal's triangle 243  
complement xvi  
complementary events xviii, 219  
completing the square 106–7, 120, 124  
concavity 88, 138  
conditional probability 197–202, 203, 219  
coordinates of midpoint 71–2  
cosine of an angle, unit circle definition 7–8, 159  
cosine function 159  
positive or negative? 169

cosine ratio xiii–xiv  
cosine rule xiv, 16–9, 21–2  
counting 235–45  
cubic functions 129–134  
cyclic quadrilateral 19

## D

degrees, converting to radians 39–40  
dependent variable xi  
direct proportion (direct variation) viii, 67  
discriminant 122  
distance between two points 72, 73  
domain 53, 54, 55, 139

## E

elements xvi  
empirical probability xviii  
equally likely outcomes xviii  
equation of a circle 148–151  
equation of a straight line 64–70, 75–7  
exact values (trigonometry) 26–8, 171–3

## F

factorials 237–8  
function notation xi  
functions xi, 53–4, 56–9  
general 142–7  
graphs of 56, 57  
linear xi, 63–81  
machine analogy xi, 55  
natural domain 55  
polynomial 129–35  
quadratic xii, 85–107  
reciprocal ix, xii–xiii, 136–7  
trigonometric 157–73  
types of xi–xiii

## G

gradient  
line joining two points 70, 72, 73  
parallel lines 80  
perpendicular lines 80–1  
straight line graphs 64–6  
graphs  
cubic functions 130  
functions 56, 57  
quadratic functions 86–98  
reciprocal functions xii–xiii, 136–7  
trigonometric functions 157–68

## H

hexagonal numbers 244  
horizontal inflection 138  
horizontal lines 66  
hyperbolas 136  
hypotenuse xiii

## I

implied domain of a function 55  
independent events 218, 219, 221–3, 226–7  
independent variable xi  
intersection (sets) xvi  
inverse proportion viii–ix

## L

length of the line joining two points 72, 73  
line symmetry 139  
line of symmetry 86, 88, 91, 94, 96  
linear functions xi, 63–81  
lines parallel to the axes 66–7

**M**

many-to-one function 53, 54  
maximum turning point 88, 94, 96, 138  
minimum turning point 86, 88, 94, 96, 138  
multiplication principle 236–8  
multiplication rule for probabilities 210, 218  
mutually exclusive events 209, 210, 218,  
219, 221, 227–8

**N**

natural domain of a function 55  
“not” in probability questions 205  
numbers, types of vii

**O**

odd functions 158, 160  
one-to-one function 53, 54  
opposite (right-angled triangle) xiii  
“or” in probability questions 205  
order of the polynomial 129

**P**

parabolic shape 86, 148  
parallel lines, gradient 80  
parity of the integer 159  
Pascal’s triangle x, 243–5  
and combinations 243  
pentagonal numbers 244  
period 158, 159, 162–3  
permutations 238  
perpendicular lines, gradient 80–1  
phase 159  
points of inflection 138  
polygonal numbers 244  
polynomial functions 129–35  
cubic functions 129–35  
probability xvii–xviii, 193–4, 196–230  
conditional 197–202, 203, 219  
empirical xviii  
independent events 218, 219, 221–3, 226–7  
mutually exclusive 209, 218–219, 221,  
227–8  
tree diagrams 203–4, 208–17  
probability questions, terminology 205  
probability rules 210, 218–19  
Pythagorean identity 178–80  
Pythagorean theorem xiii–xiv

**Q**

quadrants 130, 169  
quadratic equations 114–24  
quadratic formula 121–2, 124  
quadratic functions xii, 85–107, 115  
transformations 135

**R**

radians 38–9, 40–49  
converting to degrees 39, 40  
range 53, 54, 55, 139  
real numbers vii  
reciprocal functions ix, xii–xiii, 136–7,  
139–40  
rotational symmetry 139

**S**

sample space xviii  
scientific notation vii  
sector area 33, 34, 35, 43–49  
segment area 34, 35, 37, 43–49  
sets xvi–xvii, 195–6  
sine of an angle, unit circle definition  
5–6, 157  
sine function 157  
positive or negative? 169, 170  
sine ratio xiii–xiv  
sine rule xiv, 13–15, 20–1  
sketching, graphs 92  
quadratic functions 92–8  
cubic functions 132–4  
SOHCAHTOA xiv  
square numbers 244  
standard form vii  
straight line graphs 61–6, 68–9  
and direct proportion 67, 70  
lines parallel to the axes 66–7  
subsets xvi  
subtending an angle at a point 19

**T**

tangent function 160–1  
positive or negative? 170  
tangent ratio xiii–xiv  
three figure bearings xv  
transformations  
cubic functions 135  
general function  $y = f(x)$  142–7  
quadratic functions 135

**tree diagrams** xviii, 203–4

showing probabilities 208–17

triangle, area xiv, 9–12

triangular numbers 244

trigonometric complementarity 182

trigonometric equations 173–80, 186

trigonometric functions 157–72

graph of 157–68

trigonometric identities

angle sum and difference identities  
181–3

Pythagorean identity 178–80

trigonometric ratios xiii–xiv

trigonometry xiii–xv, 3–4

accuracy in questions xv

applications 22–25

cosine rule xiv, 16–9, 21–2

exact values 26–8, 171–3, 183–5

sine rule xiv, 13–15, 20–1

turning points 88–9, 91–6, 138

**U**

union (sets) xvi

unit circle 5–8, 157–61

universal set xvi

**V**

Venn diagrams xvi–xvii, 197, 199

vertical line test 56, 148, 158

vertical lines 67

**X**

$x$ -axis intercepts 94, 138

**Y**

$y = ax^2 + bx + c$  86, 91, 96, 98, 106–7

$y = a(x - b)(x - c)$  86, 91, 94–5, 97

$y = a(x - b)^2 + c$  86, 91–4, 97, 106–7

$y = \cos x$  159, 164

$y = f(x)$ , transformations 142–7

$y = \sin x$  157–8, 163

$y = \tan x$  160–1, 165

$y$ -axis intercepts 64–5, 91, 94, 138

$y^2 = x$  148, 150–1